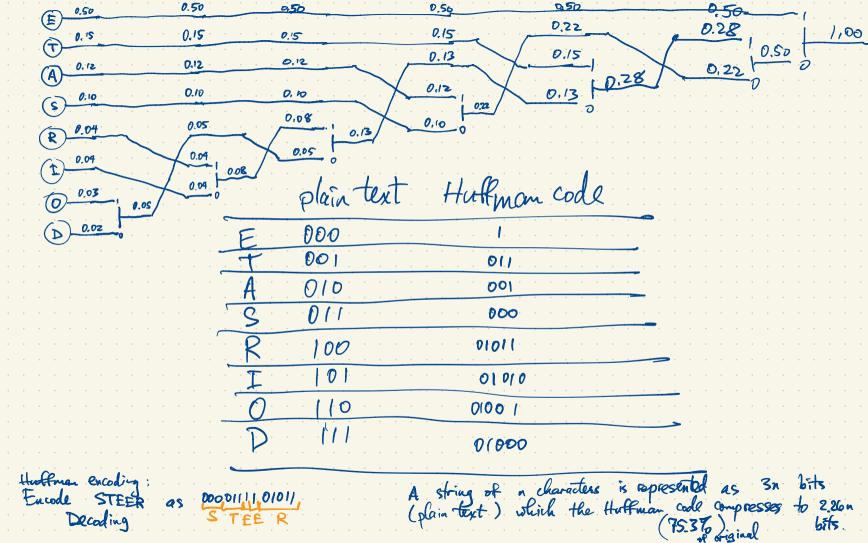


Shannon information theory classical information	etion (star	tistical	mea	gurer	west	6f	infe) FBW CI	tion	, (a	nten	ŧţ	٠		
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Example 2 of Huthman coding: Stream of 0's and 1's X= Huffman code $X = \begin{cases} 0 & \text{with polity} \\ 0 & \text{with polity} \end{cases}$ (binomial distribution) No compression Take pairs of kits Hattonan code Plain text On average, a plain text file of n bits encodes as 17 n = 0,9444 n bits Plain text Huffman code Better encode triples of bits 110 111 - 4/27 110 - 4/27 101 - 4/27 011 - 1/27 10 i דדע 0111 100 100 0110 010 010 -3/27 001 0101 000 0100 00 2/27 3/21 On average, n'bits is encoded as 76 n bits What is the limit of the compression ratio (as the block size -> 0.9383 n bits.

0.9183 n bits is the limit for compressing n bits from this stream

Shannon's first theorem showed that this stream has an entropy of $H(x) = \frac{1}{3} \log \frac{1}{\sqrt{3}} + \frac{20}{3} \log \frac{1}{2\sqrt{3}} \approx 0.9183$

Example 1 Huffman code with blocksize I character gives n bits $\rightarrow \frac{226}{3}$ n bits ≈ 0.753 n bits Entropy: Sp. logp: = 1.55678 bits per character P: = 0.5, 0.15 ..., 0.12 (i=1,2,...,8)
Compare: plain text encoding of character requires Binary entropy function: A biased coin has heads with prob. p 0
With independent tosses

H (coin) = p log + (1-p) log = 1-p = no. of bits (on average) to express the outlant

each coin flip. Recall: If X is a random variable with outcomes X= x: (1≤i≤n) with prob P: (Ep:=1) 1 HCP then the binary entropy of X is H(X)= & p. log in = no. of bits on average required to express observed values of X. when expressing information in base q the grany entropy function $H_{q}(X) = \sum_{i=1}^{n} f_{i} \log_{q}(\frac{1}{p_{i}}) = \frac{1}{\log_{q}} H_{z}(X)$ Starting Friday, more to CR144

If X can be encoded using N bits then it takes N bytes. If I buy a deck of cards its entropy is 0 in the sease that no information is required to express the order of the deck. After shuffling the deck, it takes 225.58 bits to express the order of general jobers log 52! at 225.58 221 to 19.52! at 225.58 221 the order ignore jobers log 52! at 225.58 221 the 1.8 1 the 7.8 minute video linked on course website (about 68 decimals). 2nd law of Termedynamics Wotch the 7-8 muite video linked on course website p. 49 Shamon's Source Coding Theorem (for channel without noise)

Eg. X is a stream of characters E,T,...,D (first example) with prob. 0.50,0/5..., 0.02, H(X) = 1.55 bits/der.

If I transmit into from this source using a channel with capacity 21 bits/sec. then

I can gately transmit loss that (31 bits/sec = 20 char./sec.

We can get within any pos & of this optimal rate i.e. 20-E.

2 = 256

Eg A byte is 8 bits