

If $1+1+\cdots+1\neq 0$ for any $n\geqslant 1$, then we say n has characteristic 0.

Given a field F, char F = characteristic of F is either 0 or p (some grime p).

If then $F \supseteq F = field of order <math>p$ ($F = 2/p Z = \{0,1,2,\cdots,p-1\} = "integers mad <math>p'$).

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We have been talking about number fields: finite extensions $E \supseteq Q$ i.e. $(E:Q) = n < \infty$. (Some are Galois i.e. $G = Aut \not = gatisfies |G| = n$; but in general $|G| \le n$)

If F has characteristic n > 0 then n must be prime. If n = ab, $a, b \ge 1$ then $(1+1+\cdots+1)(1+1+\cdots+1) = 1+1+1+\cdots+1 = 0$ n = ab

By minimidaly of n , n is prime.

Back to bassies:

In a field F, if $1+1+1+\cdots+1=0$ then the smallest n for which this occurs is the characteristic of F.

In either case F has a unique smellest subfield, either F or Q, called the grine subfield of F.

All fields of characteristic D are infinite. (They are extensions of Q, hance vector spaces over Q.)

If E 2F is a field extension (i.e. F, F are fields with F a subfield of E) then

E is a vector space over F. The diemension of this vector space is the degree [E:F] of this extension eq. [C: R] = 2 [C:Q] = [C:R][R:Q] =91, i & basis are la indep. for fields of characteristic a prine p, some are finite, some are infinite.

Given p prine and k > 1 (positive integer), there is a unique field of order q=pk (up to isomorphism) 一眼,睛,睛,睛,睛,睛,睛,睛, 0+10 = (1+1)0 = 00 = 0