

A group is a set & with a binary operation * which has an identity element; the	
operation is associative; and every element has an inverse. Eq. IR = set of real numbers under addition '+'. It's identify element is 0.	
0 + x = x (x+y)+z = x+ (y+z) (
$x + (-x) = 0 = (-x) + x$ for all $x, y, z \in \mathbb{R}$	
(R, +) is a group. (R, *) ireal numbers under multiplication is almost but not quite a group. (O does not have	è Con
inverse). I is the identity $\mathbb{R}^{\times} = \{all nonzero real numbers} \} = \{a \in \mathbb{R} : a \neq 0\}$ is a group mider nultiplication.	
a = a (ab)c = a(bc) $a \cdot \overline{a'} = \overline{a'}a = 1$ $\overline{a'} = \frac{1}{a}$ for all $a, b, c \in \mathbb{R}^{\times}$.	
(R ^e , x) is a group.	
R with the experision $x \star y = x + y + 7$. This is a group (\mathbb{R}, \star) . For all $x, y, z \in \mathbb{R}$, $(x \star y) \star z = (x + y + 7) + z + 7 = x + y + z + H = x + (y + z + 7) + 7 = x \star (y \star z)$ (\mathbb{R}, \star) is associative. Note that $-7 \in \mathbb{R}$ is an identify element since	· · · ·
$-7 + x = (-7) + x + 7 = x$ and $x + (-7) = x + (-7) + 7 = x$ for all $x \in \mathbb{R}$. So $-7 \in \mathbb{R}$ is an identity element for '*'.	
(-x-14) * x = (-x-14) + x + 7 = -7 $x * (-x-14) = x + (-x-14) + 7 = -7$ for all $x \in \mathbb{R}$. So $-x-14$ is an inverse element for x.	

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GL (R) = { invertible was motives with real entries } is the general linear group
$GL(R) = \left\{ \begin{bmatrix} a & b \\ c & d \end{bmatrix} : abc d \in R, ad-bc \neq 0 \right\}, I = \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \frac{1}{atbc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$
GI (R) is a multiplicative group with identity I=
GL_ (R) is not commutative for n>2.
GL (R) is commutative.
$(G, *)$ is Abelian if $x * y = y * x$ for all $x, y \in G$. (abelian)
$GL_n(\mathbb{R})$ is abelian for $n=1$, nonabelian for $n\geq 2$. $\begin{bmatrix} 1&3\\-1&7 \end{bmatrix} \begin{bmatrix} 2&0\\1&5 \end{bmatrix} = \begin{bmatrix} 5&15\\-5&35 \end{bmatrix}$ whereas $\begin{bmatrix} 2&0\\1&5 \end{bmatrix} \begin{bmatrix} 1&3\\-1&7 \end{bmatrix} = \begin{bmatrix} 2&6\\-q&38 \end{bmatrix}$.
Gl, (R) ~ R* likese are somorphic groups i.e. essentially the same group. Since R* is abelian, so
is bely (IR))
h g g f
$X \longrightarrow Y \longrightarrow Z \longrightarrow W$ If $x \in X$ then $h(x) \in Y$, $g(h(x)) \in L$, $\mathcal{T}(g(h(x))) \in W$.
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Because matrix multiplication is expressing the composition of linear transformations, it is associative
but not necessarily committative.
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