Math 2200-01 (Calculus I) Spring 2020

Book 2



Suppose a stone is thrown vertically upward from the edge of a cliff on Earth with an initial velocity of 19.6 m/s from a height of 24.5 m above the ground. The height (in meters) of the stone above the ground t seconds after it is thrown is $s(t) = -4.9t^2 + 19.6t + 24.5.$ a. Determine the velocity v of the stone after t seconds. b. When does the stone reach its highest point? c. What is the height of the stone at the highest point? d. When does the stone strike the ground?

St1 = -4962+196+24.5, 05+5

Sec 3.6 #24

beight of the stone above the ground in meters, at time t (in 6) ver = s'H) = -9.8t + 19.6, 0<t<5

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e. With what velocity does the stone strike the ground? Excords).

v10) = 19.6 m/sec is the initial velocity. In this poolen, velocity at time t (in m/sec).

the anotion is vertical with the positive direction being upwords.

(b) The stone reaches its highest point at the moment when the relocity changes sign for positive (upwards) to negative (downwards). At this moment the instanteneous velocity is zero. Solve

vet) = -9.8t + 19.6 = 0 to find t= 2 sec.

f. On what intervals is the speed increasing?

Note: S(0) = 24.5 m is the initial height;

(c) The maximum height is S(2) = 44.1 m.

(d) The stone strikes the ground when $S(t) = -4.9t^2 + 19.6t + 24.5 = 0 = -4.9(t^2 - 4t - 5) = -4.9(t - 5)(t + 1)$

this has two roots t=-1,5 sec. But since t>0, we must have t= 5 sec as the time when the stone hits the ground (e) The stone hits the ground with velocity v(5) = -29.4 m/sec (i.e. downwards at a speed of (f) Speed is increasing during the time internal 2<t<5 seconds. Remark a(t) = v'(t) = 3'(t) = -9.8 m/sec2 is constant. Sec 3.7 Chain Rule Eg. find de Sin (ex). In general if f(x) = g(h(x)) and we know g', h', how do we find f'? In other words, if x h > u + g > y - dependent variable

As an example, think of u= ex, y= sin u

independent variable - intermediate variable give rise to small changes Du in u, giving small changes by in y. Small changes Ax in x This revers to average rates of change. To get instantaneous rates of change, let \$x -> 0 so \$\Delta u > 0\$ and \$\Delta y > 0\$ giving $\frac{\Delta y}{\Delta x} = \frac{\Delta y}{\Delta u} \frac{\Delta u}{\Delta x}$ dy = dy du dx Mar 3

$$x \mapsto u = e^{x} \quad y = \sin u = \sin(e^{x})$$

$$du = du \quad du = \cos u \cdot e^{x} = e^{x} \cos(e^{x})$$

$$\frac{dy}{dx} \quad du \quad du$$

$$\frac{dy}{dx} \quad du$$

$$\frac$$

 $Eg. \frac{1}{Bx} \sin(e^x) = e^x \cos(e^x)$

Use the table to compute the following derivatives.

a.
$$h'(1) = f'(g(x))g'(x)$$

$$= f'(4) \cdot 9 = 7 \cdot 9 = 63$$

$$= f'(1) \cdot 7 = (-6) \cdot 7 = -42$$

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$$= f'(3) \cdot 9 \cdot 3$$

$$=$$

26. Derivatives using tables Let h(x) = f(g(x)) and k(x) = g(g(x)).

(a) h(x) = f(g(x))

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															(-+	(1)					(*	+1)			1 /				
						=	3	(22	*	<i>C</i> 05	(-	3×2+	 -1)																