Math 2200-01 (Calculus I) Spring 2020

Book 2



Suppose a stone is thrown vertically upward from the edge of a cliff on Earth with an initial velocity of 19.6 m/s from a height of 24.5 m above the ground. The height (in meters) of the stone above the ground t seconds after it is thrown is $s(t) = -4.9t^2 + 19.6t + 24.5.$

a. Determine the velocity v of the stone after t seconds.

- b. When does the stone reach its highest point?
- c. What is the height of the stone at the highest point?
- d. When does the stone strike the ground?
- e. With what velocity does the stone strike the ground?
- f. On what intervals is the speed increasing?

Note: S(0) = 24.5 m is the initial height;



the motion is vertical with the positive direction being upwards. (b) The stone reaches its highest point at the moment when the velocity changes sign for positive (upwards) to negative (down wards). At this moment the instanteneous velocity is zero. Solve vet) = -9.8t + 19.6 = 0 to find t= 2 sec.

(c) The maximum height is S(2) = 44.1 m. (d) The stone strikes the ground when $S(t) = -4.9t^2 + 19.6t + 24.5 = 0 = -4.9(t^2 - 4t - 5) = -4.9(t^2 - 4t - 5)(t + 1)$

this has two roots t=-1,5 sec. But since t>0, we must have t= 5 sec as the fine when the stone hits the ground. 1e) The stone hits the goand with velocity v(5) = -29.4 m/sec (i.e. downwards at a speed of 29.4 m/sec). (f) Speed is increasing during the time interval 2<t<5 seconds. Remark all = v'(1) = 9"(1) = -9.8 m/sec² is constant. Sec 3.7 Chain Rule Eg. find $\frac{d}{dy_{x}}$ Sin (e^x). In general if f(x) = g(h(x)) and we know g', h', how do we find f'? In other words, if $x \downarrow h \Rightarrow u \downarrow g \Rightarrow y = dependent variable$ g g g g dependent variableAs an example, thick of u= ex, y= sin uindependent variablegive rise to small changes Δu in u, giving small changes Δy in y. Small changes Ar in x This refers to average rates of change. To get instantaneous rates of change, let \$x=0 so \$44 =0 and \$4y=0 giving $\frac{\Delta y}{\Delta x} = \frac{\Delta y}{\Delta u} \frac{\Delta u}{\Delta x}$ $\frac{dq}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$