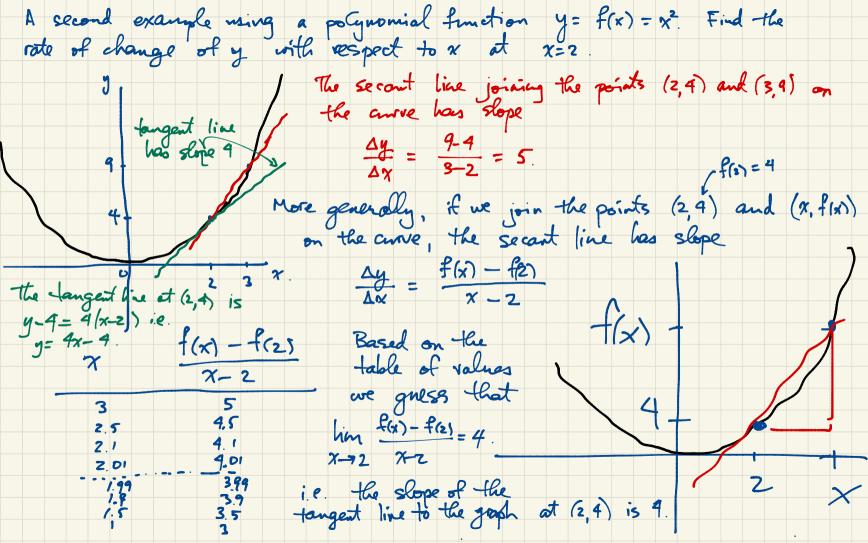
Math 2200-01 (Calculus I) Spring 2020

Book 1

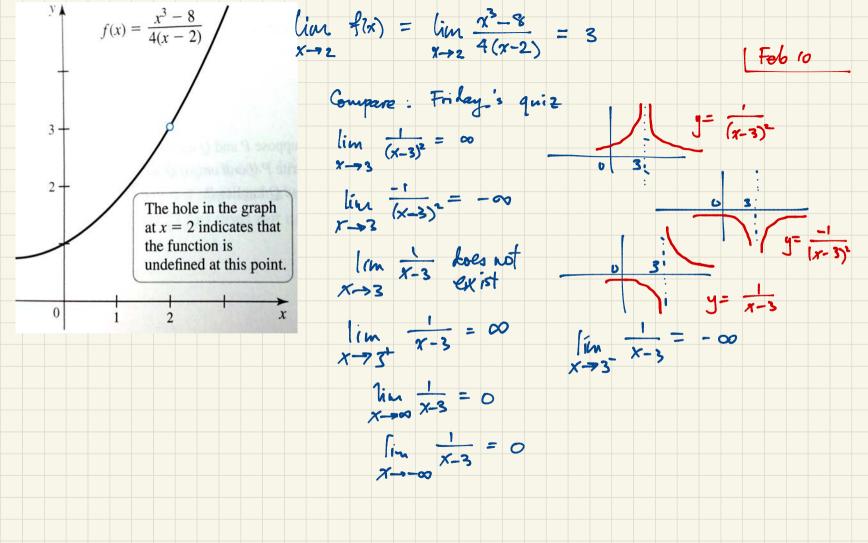


Calculus I: Single variable calculus y= f(x) for example (one input variable x, one output variable). Derivatives (votes of change): differential calculus. Calculas II - also single-variable. Integral calculus. Calculus III: multivariable ie. several iaput variables and/or several output variables
eg. position (xrt), yrt), zrt) of an object at time t: one imput t, three output
variables xrt), yrt), zrt). Eg. Temperature in this room as a function of position T(x,y,z) (three inputs x,y,z; one output T) Eg. Wind relocity as a function of position: three inpits x, y, z; three outputs are the components of wind relocity. Jan 2 Tangent line There is second line There is tangent line here

- Temperature T as a function of fine t During the time interval [4., t2] i.e. t, \le t \le t_2 The average rate of change of temperature during this time iterval is $\Delta T = T_z - T_i$ change in temperature $\Delta t = t_z - t_i$ time elapset (t, T,) to (t, T,) on the graph. We want to under stand the instantaneous rate of change of temperature at time to To determine this, first consider the average vate of change over smaller and smaller time intervals [t, fz] where we take to - t. (to gets closer and closer to ti). We write $\lim_{t\to 3} \frac{t-t_1}{t-t_1} = 2.2$ 4 2 dogress/hour The (iant is 22 (the limit of T2-T1 is 2.2 The temperature at 3pm is changing at a rate of 2.2 degrees per hour. as to approaches 3). 2.23 2.31



It a function has a sufficiently vice formula of polynomial, then we have algebraic rules that provide definite ways to evaluate limits, eliainating guesswork based on the graph or table & values. Eg. Find the slope of the tangent line to the graph of $y = x^2$ at (2,4). Solution The secont line from (2,4) to $(x, f(x)) = (x, x^2)$ has slope $\frac{\Delta y}{\Delta x} = \frac{x^2 - 4}{x - 2} = \frac{(x + 2)(x - 2)}{x - 2} = x + 2$ The slope of the tangent line is $\lim_{x\to 2} \frac{x-4}{x-2} = \lim_{x\to 2} (x+2) = 2+2=4$ Both of these Sunctions satisfy $\lim_{x\to 2} f(x) = 4$ Both of these Sunctions satisfy $\lim_{x\to 2} f(x) = 4$



A function f is continuous at a if him flx) = fa). Sec 2.6 Explicitly, this requires that x-ra $f(x) = \frac{x}{x^2 - 7x + 12}$ (1) I must be defined at a, ie. Isa) exists; (iii) the values in (i) and (ii) must agree Eg for the function of on the right · f is his continuous at 5; · · · · · · · 3. +(3) = 1, lim fixt does not exist. Continuous everywhere except x = 3 and x = 4· f is not continuous at 2. f(2)=3, lian f(x) = 1 but these two values do not agree! Although lim f(x) = 3, fis not . I is discontinuous at 1. defined at 1. 7 is continues on (0,7) i.e. 0<x<7 except at 1,2,3,5.

Eg. the cost of parking at a meter is 25 th for each 1.25 -15 minutes The cost (it) as a function of time Cost (dollars) 0.75 - 0.50 is discontinuous at f = 0, 15, 80, 45,60,... At each of these points of discontinuity, c is left-continuous (i.e. lien f(t) = f(a)) but not right-continuous 0.25 (i.e. $\lim_{t\to a^+} f(t) \neq f(a)$). Time (min)